

*Understanding  
the UV-visible-NIR scattering  
of non-spherical  
metallic nanoparticles*



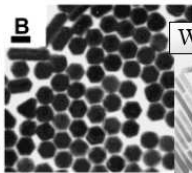
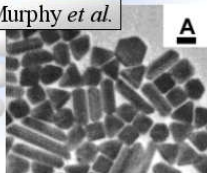
Stuart W. Prescott, Paul Mulvaney

Particulate Fluids Processing Centre  
School of Chemistry  
University of Melbourne

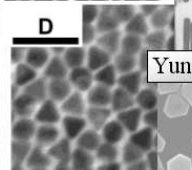
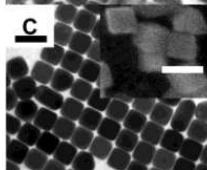
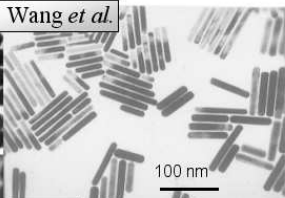


# Recent synthetic achievements

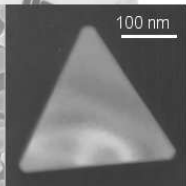
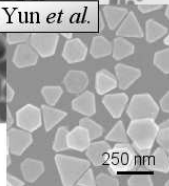
Murphy *et al.*



Wang *et al.*



Yun *et al.*



scale bars = 100 nm



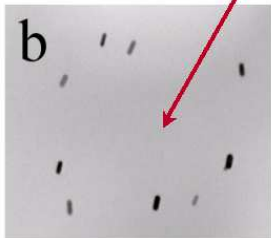
# Uses of nanorods

Au nanorods (AR  $\sim 2.9$ ) in a PVA film

randomly oriented



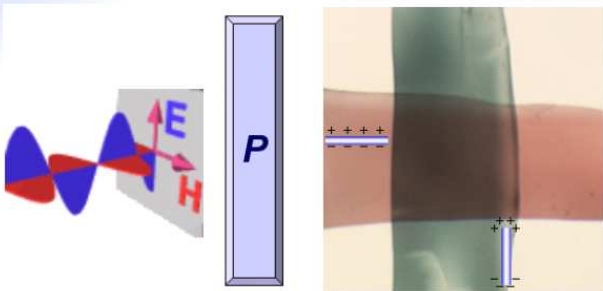
after PVA stretched

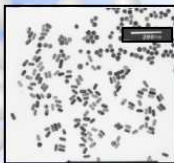


# Uses of nanorods

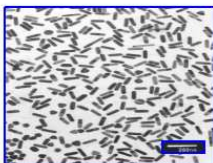
Stretching of PVA aligns rods

- photograph under polarised light:





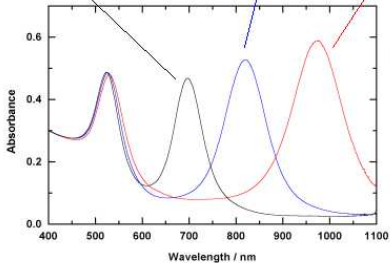
*A.R.: 2.25*  
*Width: 20.7 nm*  
*Length: 46 nm*



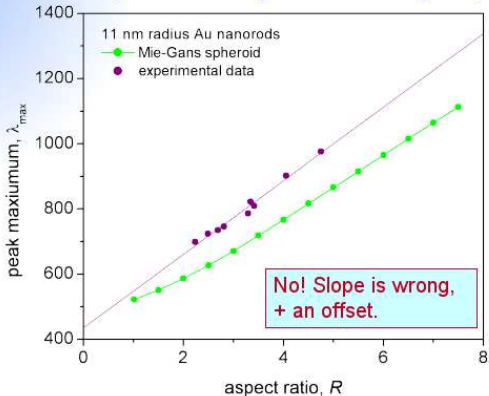
*A.R.: 3.35*  
*Width: 22.4 nm*  
*Length: 75 nm*



*A.R.: 4.75*  
*Width: 22.8 nm*  
*Length: 108 nm*



# Are these prolate spheroids (ellipsoids)?

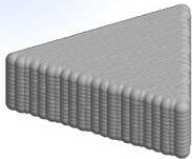


All spectra are for gold nanorods in water



## Correctly predicting $\lambda_{\max}$

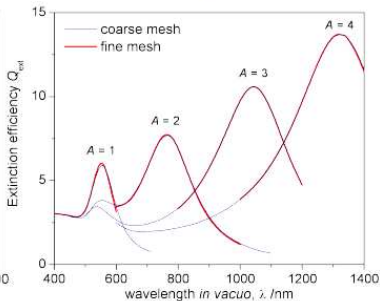
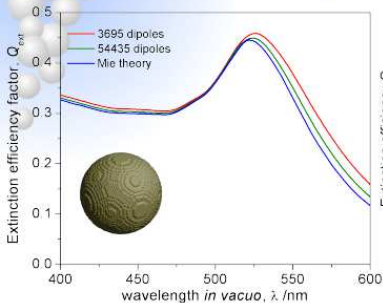
Investigating influence of  
particle shape and size:



Discrete Dipole Approx. Model

Cubic array of dipoles (Draine & Flatau)

# Checking DDA for nanoparticles



DDA captures  
target and  
spectrum features



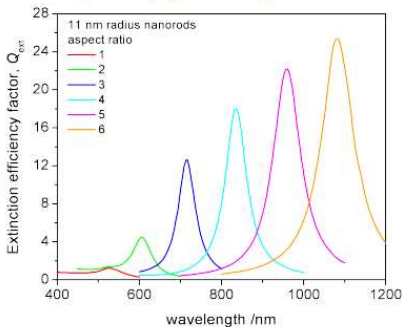
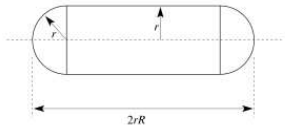
34189 dipoles  
294293 dipoles



# DDA for Au spherically capped cylinders

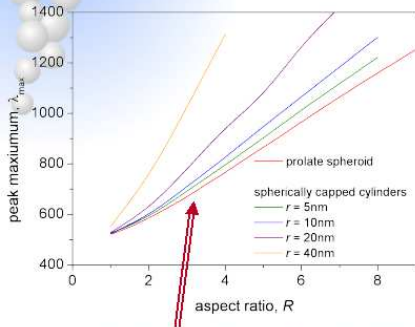
For aspect ratio,  $R$

- spherical end cap, radius  $r$
- particle length  $2rR$
- cylinder length  $2r(R-1)$



$\lambda_{max}$  varies with  $R$ , and becomes more intense

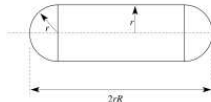
# $\lambda_{\max}$ varies with rod width?



prolate spheroid,  $R = a/b$



spherically capped cylinder



$\lambda_{\max}$  independent of rod width  
for Mie-Gans prolate spheroid

Also recently reported by Brioude, *et al.*,  
*J. Phys. Chem. B*, 109, 13138, 2005.



# Spectra & Geometrical Factors

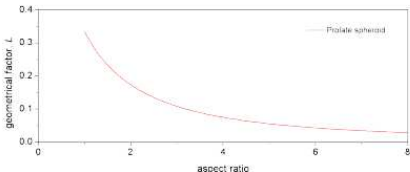
Polarisability,  $\alpha$ , gives extinction:

- single parameter expression for  $Q_{\text{ext}}(\lambda)$
- geometrical factor  $L$  (sphere has  $L=1/3$ )

$$\alpha = V \frac{\epsilon - \epsilon_m}{\epsilon_m + L(\epsilon - \epsilon_m)}$$

$$Q_{\text{ext}}(\lambda) = \frac{2\pi\sqrt{\epsilon_m}}{G\lambda} \text{Im}\{\alpha\}$$

$$Q_{\text{ext}}(\lambda) = \frac{2\pi V \epsilon_m^{3/2}}{GL^2\lambda} \frac{\epsilon''}{\left(\epsilon' + \frac{1-L}{L}\epsilon_m\right)^2 + (\epsilon'')^2}$$

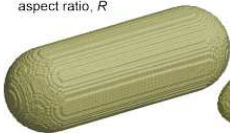
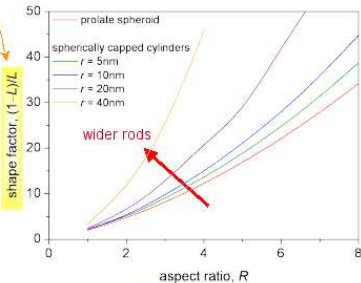
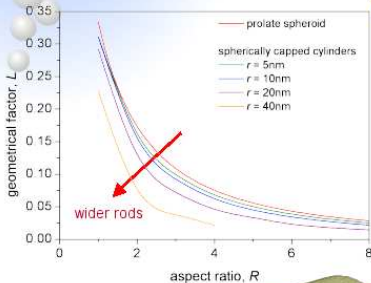


( $L$  shown for longitudinal mode only)

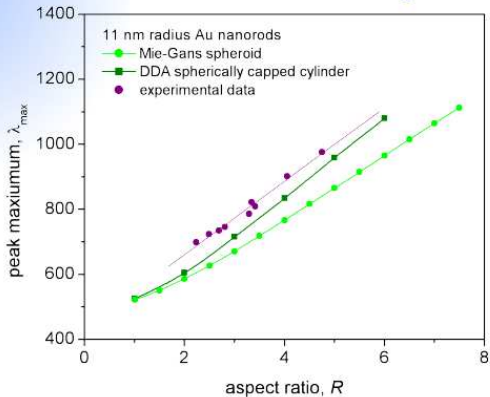


$$Q_{\text{ext}}(\lambda) = \frac{2\pi V \varepsilon_m^{3/2}}{GL^2 \lambda} \frac{\varepsilon''}{\left(\varepsilon' + \frac{1-L}{L} \varepsilon_m\right)^2 + (\varepsilon'')^2}$$

## *L and rod width*



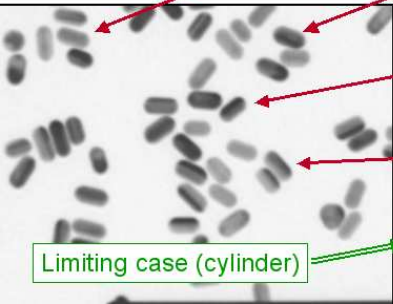
# DDA gets closer...



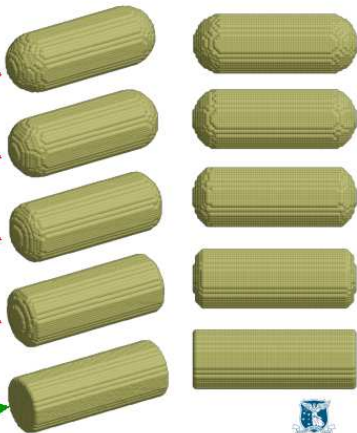
... but there is room for improvement

# End-cap effects

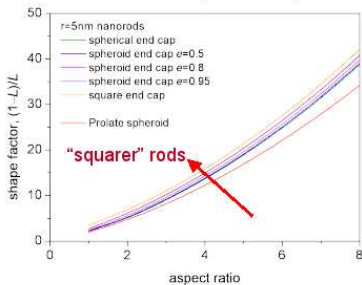
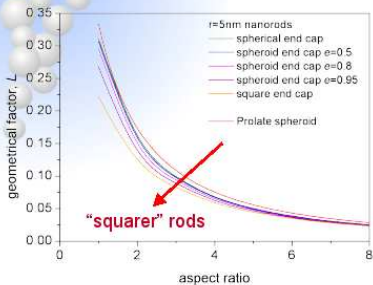
Does end-cap geometry change spectrum?



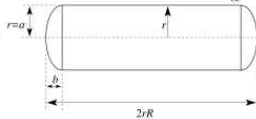
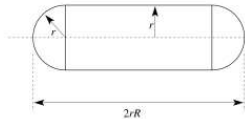
Limiting case (cylinder)



# *L and end-cap shape*

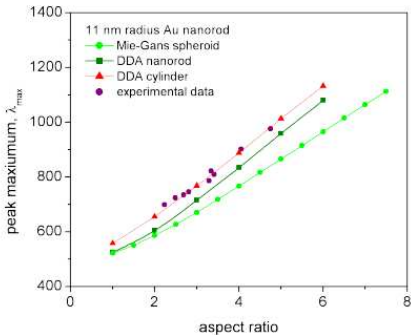
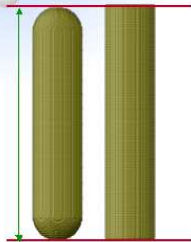


For the spheroid end caps, eccentricity:  $e^2 = 1 - \frac{b^2}{a^2}$



# Limits on $\lambda_{\max}$ using DDA

$\lambda_{\max}$  should be between cylinder and rod:

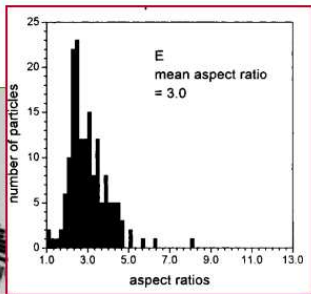
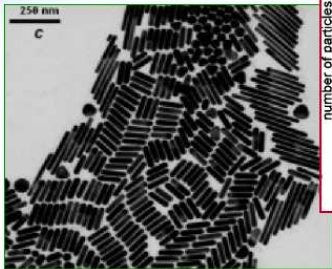


... cylinders seem to be the closest geometry?  
something must be wrong...



# Sample purity

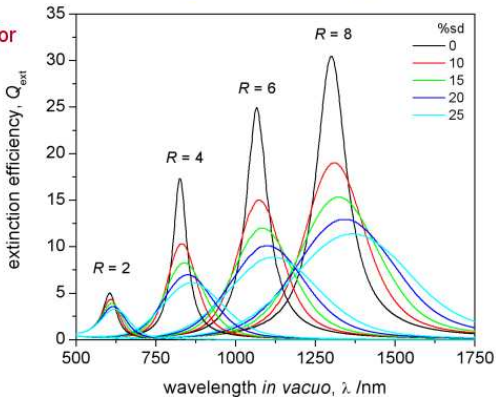
How does a distribution of rods sizes change the spectrum?



Example data from Yu *et al.*, *J. Phys. Chem. B*, 101, 6661, 1997.

# "Synthetic" spectra

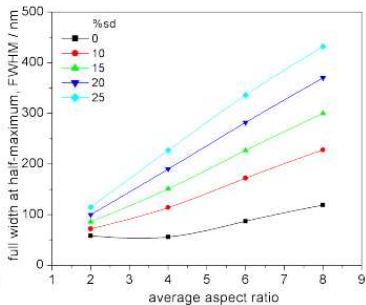
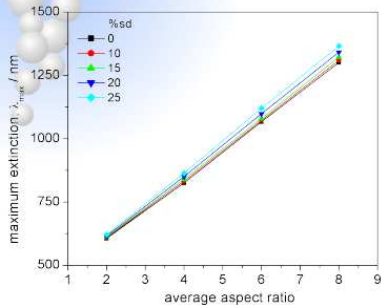
1. Find functional form for geometrical factor,  $L(R, r)$
2. Calculate spectra for each bin in discrete particle length distribution
3. Add weighted component spectra



Geometrical factor,  $L$ , becomes powerful tool



# Limits from “synthetic” spectra



- red-shift of  $\lambda_{\max}$  due to broadening of distribution
- FWHM also increases



# Conclusions: predicting $\lambda_{\max}$

Must consider:

- particle shape
  - these are nanorods *not* ellipsoids
  - width is important *not just aspect ratio*
- subtle end effects
  - spheroid end cap?
- particle size distribution
  - control it? reduce it? purify?



# Conclusions: characterisation

Spectrometric characterisation of nanorods...

- for a given aspect ratio,
  - ellipsoid model gives uniquely determined  $\lambda_{\max}$
  - DDA:  $\lambda_{\max}$  depends on width too
- with an independent measure of width...
  - ...and known end-cap geometry...
  - ...and a Gaussian distribution
  - ( $\lambda_{\max}$ , FWHM) uniquely determines
    - ❖ “light-scattering average” aspect ratio
    - ❖ standard deviation of distribution



# Acknowledgements

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Copies available from [nanonano.net](http://nanonano.net)

